

## PHYSICS 2P51: Assignment 9/10 - Due Wed. March 29, 2017

### 1. Michelson interferometer

- (a) Consider a Michelson interferometer using a source of 632.8 nm light. What is the displacement of the moving mirror if 2500 fringes cross the center of the interference pattern?
- (b) If one arm of a Michelson interferometer contains a tube 3.5 cm long that is first evacuated and then slowly filled with air ( $n = 1.0003$ ), how many fringes will cross the centre? Assume light of 600 nm wavelength.
- (c) Consider a Michelson interferometer that contains an imperfect beamsplitter which creates two interfering beams at the detector with unequal intensity:  $0.5 \text{ mW/m}^2$  and  $0.4 \text{ mW/m}^2$ . Assume a monochromatic source of wavelength 550 nm. Determine the intensity at the detector as a function of moving mirror position  $x$ . What are the maximum and minimum intensities measured?

### 2. Thin Film Inteference

- (a) A soap bubble ( $n = 1.4$ ) has a wall that is  $0.36 \mu\text{m}$  thick. If seen at normal incidence in reflected white light, what colour is it?
- (b) What percentage of incident light is reflected at the surface of a glass of index  $n=5/3$ ? If one wanted to minimize the reflectance at  $\lambda = 550\text{nm}$ , what is the minimum thickness of  $\text{MgF}_2$  ( $n = 1.38$ ) that must be deposited on the surface of the glass?
- (c) A wedge-shaped spaced between plane glass plates if filled with water ( $n = 4/3$ ) in such a way that there a few bubbles of air are trapped between the plates. If 18 fringes are counted with a given distance inside an air bubble, how many fringes, within the same distance, are seen in water?

### 3. Single slit Diffraction

- (a) How many wavelengths wide must a single slit be if the first Fraunhofer diffraction minimum occurs at an angular distance of  $30^\circ$  from the optical axis.

(b) A slit 0.14 mm wide is illuminated by monochromatic light. If on a screen 2m away from the slit, the two second-order minima are 3 cm apart from each other, what is the wavelength of the light?

4. **Real Double Slit** Recall that the intensity for two slits of width  $a$  separated by distance  $d$  varies as

$$I = I_o \left( \frac{\sin \alpha}{\alpha} \right)^2 \cos^2(\beta)$$

where  $\alpha = \pi \frac{a \sin \theta}{\lambda}$  and  $\beta = \pi \frac{d \sin \theta}{\lambda}$ . That is, it is a superposition of the single slit pattern and the equally spaced double slit fringes. Determine how many double slit maxima lie within the wide central single slit fringe.