

Electric Dipole Radiation - point dipole

1. Show that for a point dipole, where “ \sim ” means to approach asymptotically in the radiation zone,

(a)

$$\vec{E}_{rad} \sim \frac{\mu_o}{4\pi r} \left[\hat{r} \left(\hat{r} \cdot \frac{d^2\vec{p}}{dt^2} \right) - \frac{d^2\vec{p}}{dt^2} \right]$$

(b)

$$\vec{S}_{rad} \sim \frac{\mu_o}{c} \left(\frac{1}{4\pi r} \right)^2 \left[\left| \frac{d^2\vec{p}}{dt^2} \right|^2 - \left(\hat{r} \cdot \frac{d^2\vec{p}}{dt^2} \right)^2 \right]$$

2. For a Hertzian point dipole where $\vec{p} = p_o \cos(\omega t)\hat{z}$, show that

$$\vec{B}_{rad} \sim -\frac{\mu_o p_o \omega^2}{4\pi c} \frac{\cos[\omega(t - r/c)]}{r} \sin(\theta)\hat{\phi}$$

$$\vec{E}_{rad} \sim -\frac{\mu_o p_o \omega^2}{4\pi} \frac{\cos[\omega(t - r/c)]}{r} \sin(\theta)\hat{\theta}$$

$$\vec{S}_{rad} \sim \frac{\mu_o p_o^2 \omega^4}{16\pi^2 c} \frac{\cos^2[\omega(t - r/c)]}{r^2} \sin^2(\theta)\hat{r}$$

Note that these are identical to the results that Griffiths obtains, using a different method.