

## Magnetic Properties of materials

1. In the case of magnetostatics, the Maxwell equation for the curl of  $\vec{B}$  can be written,

$$\vec{\nabla} \times \vec{H} = \vec{J}_f,$$

which can be solved by the use of Stoke's theorem and the techniques used to find  $\vec{B}$  in Ampere's law. Explain what condition must be satisfied in order for  $\vec{H}$  to be determined solely by the free currents.

2. An infinitely long cylinder of radius  $R$  carries a "frozen-in" magnetization, parallel to the axis,

$$\vec{M} = ks\hat{z},$$

where  $k$  is a constant and  $s$  is the distance from the axis; there is no free current anywhere. Find the magnetic field  $\vec{B}$  inside and outside the cylinder by two different methods:

- (a) Locate all the bound currents, and calculate the field they produce.
- (b) Use Ampere's Law to find  $\vec{H}$ , and then get  $\vec{B}$  from the definition,

$$\vec{H} = \frac{1}{\mu_0} \vec{B} - \vec{M}$$